

Index

Note: Many special kinds of numbers, such as rational, prime, or perfect, can be found under the index entry “numbers.” Special constants, such as the golden ratio (ϕ), Euler’s number (e), or pi (π), can be found under the index entry “constants.”

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