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\*Sections marked by an asterisk (\*) may be skipped in a first reading (please refer to note in Preface).

