

WWW.SIMULATION: WHAT, WHY AND WHEN?



1.1 Introduction

The management of an airport are planning the facilities that are required in a new terminal building. Important decisions need to be made about, among other things, the number of check-in desks devoted to each airline, the size of the baggage handling system, the amount of security check positions and the number of departure gates. On top of this, the number of staff to employ and the shifts they should work need to be determined. The total investment is in the tens of millions and it is critical that these decisions are made correctly. How can the management determine the number of resources that are required in each area of the airport?

One approach would be to build the terminal and hope that it works! This seems very risky with so much at stake. Only slightly better would be to rely upon gut feel, no doubt based on some past experience with designing and managing airport terminals. A few paper calculations, or even a spreadsheet, may help, but these are unlikely to be able to handle the full complexity of the situation.

A much more effective approach is likely to be a simulation of the proposed airport terminal. This could imitate the flow of passengers and their bags through each of the key stages from arrival to departure and would act as a basis for planning airport facilities. Indeed, simulation models are used by many organizations to plan future facilities and to improve current ones. Manufacturing companies simulate their production lines, financial services organizations simulate their call centres and transport companies simulate their delivery networks. There are many examples of simulation being used in practice.

This chapter aims to answer three questions concerning simulation:

- What exactly is a simulation?
- Why would an organization choose to develop and use a simulation model?
- When is simulation appropriate?

1.2 What is Simulation?

Simulation models are in everyday use and so simulation is a concept that is not alien to us. For instance, weather forecasters daily show us simulations of the weather system, where we see the movement of weather fronts over the days ahead. Many of us have game consoles that simulate a whole variety of activities, enabling us to test our skills as racing drivers, adventurers and city planners. Simulations need not be computer based. Model railways and remote control boats are familiar examples of physical simulations.

So what does the term simulation mean? In its most general sense a simulation can be defined as:

An imitation of a system.

Imitation implies mimicking or copying something else. For instance, a forger imitates the work of a great artist. The Strip in Las Vegas is full of imitations: the Eiffel Tower, the New York skyline, Venice and so on. In the 2002 soccer world cup, if a player imitated being the recipient of foul play, it was referred to as a “simulation”. Computer aided design (CAD) systems provide imitations of production facility designs and a business process map is an imitation of a business organization. All of these can be described as a simulation in its most general sense.

There is, however, a key difference between these imitations and those examples described in the first paragraph of this section. The earlier examples involve the passage of time, whether it is the movement of trains on a track or clouds in a weather system. The second set of examples does not involve the passage of time. Hence there is a difference between the concepts of a *static simulation*, which imitates a system at a point in time, and a *dynamic simulation*, which imitates a system as it progresses through time (Law and Kelton 2000). The term simulation is mostly used in the context of dynamic simulation.

This book is concerned only with dynamic simulations. Further to this, the focus is on computer based simulations rather than physical simulations, although many of the principles that are described would still apply to the latter. Building on the previous definition, computer based dynamic simulation can be defined as follows:

An imitation (on a computer) of a system as it progresses through time.

Some aspects of this definition need exploring a little further. First, the concept of a *system* needs to be explained. In general terms a system is a collection of parts organized for some purpose (Coyle 1996). The weather system, for instance, is a collection of parts, including the sun, water and land, that is designed (assuming we believe in a Creator) for the purpose of maintaining life.

Checkland (1981) identifies four main classes of system:

- *Natural systems*: systems whose origins lie in the origins of the universe, e.g. the atom, the Earth’s weather system and galactic systems.
- *Designed physical systems*: physical systems that are a result of human design, e.g. a house, a car and a production facility.

- *Designed abstract systems*: abstract systems that are a result of human design, e.g. mathematics and literature.
- *Human activity systems*: systems of human activity that are consciously, or unconsciously, ordered, e.g. a family, a city and political systems.

All such systems can be, and indeed are, simulated. This book, however, is concerned with simulation as it is used for modelling in private and public sector organizations. When describing and understanding these organizations two classes of system are of prime concern, that is, designed physical and human activity systems. For instance, a simulation might be developed of an automated production facility or warehouse (a designed physical system), or at the other extreme a model of regional health care delivery (a human activity system). Many situations cannot be defined simply as either a designed physical system or a human activity system, but they lie at the interface between the two. A bank, for instance, consists of a designed physical system (the service counters, automatic tellers, etc.), but it is also a human activity system where the staff and customers interact between and with one another. Indeed, many of the situations in which simulation is used lie at the interface between designed physical systems and human activity systems. For instance, service operations (banks, call centres and supermarkets), manufacturing plants, supply chains, transport systems, hospital emergency departments and military operations all involve elements of both classes of system. In general terms, these systems can be referred to as *operations systems* or *operating systems*. “An operating system is a configuration of resources [parts] combined for the provision of goods or services [purpose]” (Wild 2002; words in brackets added by author). Wild identifies four specific functions of operating systems: manufacture, transport, supply and service.

There are, of course, cases where other types of system need to be modelled as well. For instance, in a simulation of a port it may be necessary to model the tidal and weather conditions, since adverse conditions may prevent a ship from entering the port. As such, it is necessary to model, at least simply, some natural systems. In general this would involve modelling the outcome of the natural system (e.g. high winds) rather than the system itself.

A second aspect of the definition that needs exploring further is to consider the purpose of simulation models. Pidd (2003), in a more general discussion about models in management science, identifies the purpose of models as understanding, changing, managing and controlling reality. Following this theme, the purpose of a simulation can be described as obtaining a better understanding of and/or identifying improvements to a system. Improved understanding of a system, as well as the identification of improvements, is important since it informs future decision-making in the real system.

Another feature of Pidd’s description of models is his emphasis on simplification. It is unlikely that a simulation of an operations system, particularly the elements of human activity, could represent its full detail. Indeed, even if it were possible, it is probably not desirable, since the time required to collect data on and model every aspect of a system would be excessive. Note that even the Las Vegas only built a half-size replica of the Eiffel Tower, and this for a “simple” physical structure!

A final aspect to consider is the nature of simulation model use. Some modelling approaches attempt to provide optimum answers (e.g. linear programming) or near optimum

answers (e.g. heuristic methods). This is not the case for a simulation model. A simulation simply predicts the performance of an operations system under a specific set of inputs. For instance, it might predict the average waiting time for telephone customers at a call centre when a specific number of operators are employed. It is the job of the person using the simulation model to vary the inputs (the number of operators) and to run the model in order to determine the effect. As such, simulation is an experimental approach to modelling, that is, a “what-if” analysis tool. The model user enters a scenario and the model predicts the outcome. The model user continues to explore alternative scenarios until he/she has obtained sufficient understanding or identified how to improve the real system. As a consequence, simulation should be seen as a form of decision support system, that is, it supports decision-making rather than making decisions on behalf of the user. It should be noted, however, that most modern simulation software provide facilities for automating the experimentation process with the aim of finding an optimum scenario. These facilities and their application are discussed in Section 10.5.4.

These four aspects (operations systems, purpose, simplification and experimentation) are now added to the previous definition so that simulation is defined as:

Experimentation with a simplified imitation (on a computer) of an operations system as it progresses through time, for the purpose of better understanding and/or improving that system.

This is the nature of the simulations that are described in this book. Note that some specifics of this definition are discussed in detail in later chapters, in particular, the methods of imitating a system as it progresses through time (Section 2.2), approaches to simplification (Section 6.3) and experimentation (Chapters 9 and 10). From here on the term simulation will be taken to mean simulation as defined above, unless otherwise stated.

1.3 Why Simulate?

In order to answer this question, three perspectives are adopted. First, the need to use simulation because of the nature of operations systems is discussed. Secondly, the advantages of simulation over other approaches to understanding and improving a system are described. Finally, the disadvantages of simulation are discussed, on the grounds that it is important to be cognizant of these when determining whether or not to use the approach.

1.3.1 The nature of operations systems: variability, interconnectedness and complexity

Many operations systems are subject to *variability*. This might be predictable variations, for instance, changing the number of operators in a call centre during the day to meet changing call volumes or planned stoppages in a production facility. It might also be variations that are unpredictable, such as the arrival rate of patients at a hospital emergency department or the breakdown of equipment in a flexible manufacturing cell. Both forms of variability are present in most operations systems.

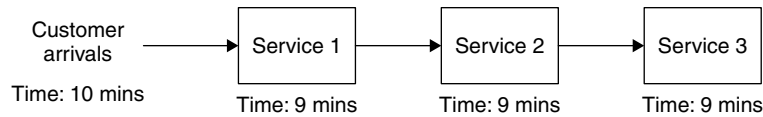


Figure 1.1 Example of an Interconnected System Subject to Variability.

Operations systems are also *interconnected*. Components of the system do not work in isolation, but affect one another. A change in one part of a system leads to a change in another part of the system. For instance, if a machine is set to work faster this is likely to cause a reduction in work-in-progress up-stream and a build-up of parts down-stream.

It is often difficult to predict the effects of the interconnections in a system, especially when variability is present. Take the following example. Customers in a service process pass through three (interconnected) stages (Figure 1.1). Each stage takes exactly 9 minutes. Customers arrive exactly every 10 minutes. What is the average time a customer spends in the system? This is a relatively simple question to answer, since there is no variability in the system. The average time customers spend in the system is 27 minutes; in fact each customer spends exactly 27 minutes in the system.

Now assume that the times given above are averages, so customers arrive on average every 10 minutes and it takes on average 9 minutes to serve a customer at each stage. What is the average time a customer spends in the system? This is not an easy question to answer since there is variability in both customer arrivals and service times. It is also expected that queues will develop between the service stages. Added to this, the range of variability around the average is not known. Most people would estimate that the average is still 27 minutes or maybe slightly longer. In fact, assuming a typical range of variability (a negative exponential distribution – Section 7.4.3), the average is near to 150 minutes. The compound effect of variability and the interconnections in the system make it very difficult to predict the overall performance of the system.

Many operations systems are also *complex*. It is difficult to provide an exact definition of the word complexity; an interesting discussion can be found in Gell-Mann (1994) and in relation to simulation and modelling in Brooks and Tobias (1996). For our purposes it is useful to distinguish between *combinatorial complexity* and *dynamic complexity*. Combinatorial complexity is related to the number of components in a system or the number of combinations of system components that are possible. The travelling salesman problem is a useful illustration of this. A salesperson has to make a series of visits to potential customers during a day. The aim is to find the shortest route around those customers. If there are eight “cities” (customers) to visit, then the sales person is faced with 2520 possible combinations of routes (this is calculated by $(n - 1)!/2$, where n is the number of cities). As the number of cities increases, so the number of combinations grows at an increasing rate. A 16 city tour gives 6.5×10^{11} combinations of routes! The problem is subject to combinatorial complexity.

Combinatorial complexity is present in some operations systems. Take, for instance, a job shop. Parts are processed through a series of machines. Once the processing is complete on one machine, a part is passed to any one of the other machines, depending on the type of part and the next process required. The more machines there are in the job shop, the more the

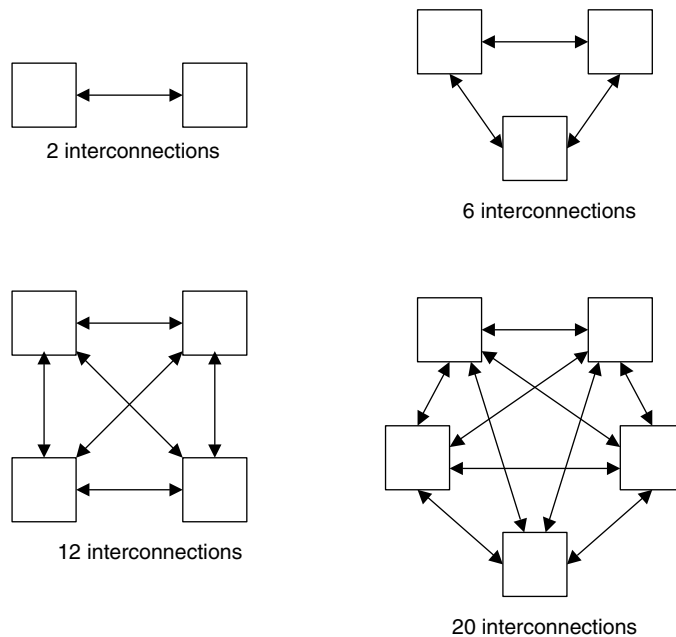


Figure 1.2 Job Shop Systems: Interconnections and Combinatorial Complexity.

potential interconnections. As the number of machines increases so the interconnections increase at an even faster rate. Figure 1.2 shows the possible interconnections for job shops with two, three, four and five machines. There are two interconnections between any two machines since parts can move in either direction. The total number of interconnections can be calculated as $n(n - 1)$, where n is the number of machines in the job shop.

On the other hand, dynamic complexity is not necessarily related to size. Dynamic complexity arises from the interaction of components in a system over time (Sterman 2000). This can occur in systems that are small, as well as large. Systems that are highly interconnected are likely to display dynamic complexity.

Senge (1990) illustrates dynamic complexity with the “beer distribution game”. This represents a simple supply chain consisting of a retailer, wholesaler and factory. The retailer orders cases of beer from the wholesaler, who in turn orders beer from the factory. There is a delay between placing an order and receiving the cases of beer. The game demonstrates that a small perturbation in the number of beer cases sold by the retailer can cause large shifts in the quantity of cases stored and produced by the wholesaler and factory respectively. Such a system is subject to dynamic complexity.

Senge (1990) describes three effects of dynamic complexity:

- An action has dramatically different effects in the short and long run.
- An action has a very different set of consequences in one part of the system to another.
- An action leads to non-obvious consequences (counter intuitive behaviour).

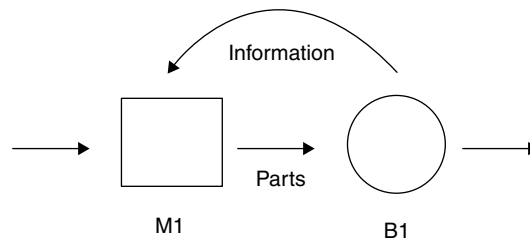


Figure 1.3 Simple Kanban System Demonstrating Feedback.

These effects make it very difficult to predict the performance of a system when actions are taken, or changes are made.

The effects described above often arise because of feedback within a system. Feedback occurs when the components of a system are interconnected in a loop structure. As a result an action taken at one point in a system eventually leads to a feedback effect on that same point in the system. A simple example is a kanban system (Figure 1.3). Machine M1 feeds buffer B1. The rate at which M1 works depends upon the number of parts in B1. The smaller the inventory in B1 the faster M1 works, and vice versa. M1 is connected to B1 through the flow of parts and B1 is connected to M1 through the flow of information about the quantity of parts in the buffer. There is, therefore, a loop structure and so feedback occurs. For instance, if M1 is made to work faster, this increases the number of parts in B1, which in turn reduces the speed at which M1 works. This is, of course, a very simple example.

The interconnections in operations systems are often not unidirectional, and so loop structures and feedback are quite common. In particular, physical items and information often flow in opposite directions. In a supply chain, for instance, physical items often move towards the customers while information about orders for more stock move towards the producers. In some cases the loop structures are very complex, involving many system components.

The need for simulation

Many operations systems are interconnected and subject to both variability and complexity (combinatorial and dynamic). Because it is difficult to predict the performance of systems that are subject to any one of variability, interconnectedness and complexity, it is very difficult, if not impossible, to predict the performance of operations systems that are potentially subject to all three. Simulation models, however, are able explicitly to represent the variability, interconnectedness and complexity of a system. As a result, it is possible with a simulation to predict system performance, to compare alternative system designs and to determine the effect of alternative policies on system performance.

The methods for modelling variability in simulation are discussed in Section 2.3 and Section 7.4. Section 6.2.4 discusses the need to account for the interconnections in a system. The combination of modelling variability and interconnectedness means that the complexity in a system can be represented by a simulation model.

1.3.2 The advantages of simulation

Simulation is not the only method of analysing and improving operations systems. In particular, it might be possible to experiment with the real system or to use another modelling approach (Pidd 1998). What are the specific advantages of simulation over these approaches?

Simulation versus experimentation with the real system

Rather than develop and use a simulation model, experiments could be carried out in the real system. For instance, additional check-in desks could be placed in an airport departure area, or a change in the flow around a factory floor could be implemented. There are some obvious, and less obvious, reasons why simulation is preferable to such direct experimentation.

- *Cost.* Experimentation with the real system is likely to be costly. It is expensive to interrupt day-to-day operations in order to try out new ideas. Apart from the cost of making changes, it may be necessary to shut the system down for a period while alterations are made. Added to this, if the alterations cause the operation's performance to worsen, this may be costly in terms of loss of custom and customer dissatisfaction. With a simulation, however, changes can be made at the cost of the time it takes to alter the model and without any interruption to the operation of the real world system.
- *Time.* It is time consuming to experiment with a real system. It may take many weeks or months (possibly more) before a true reflection of the performance of the system can be obtained. Depending on the size of the model and speed of the computer, a simulation can run many times faster than real time. Consequently, results on system performance can be obtained in a matter of minutes, maybe hours. This also has the advantage that results can be obtained over a very long time frame, maybe years of operation, if required. Faster experimentation also enables many ideas to be explored in a short time frame.
- *Control of the experimental conditions.* When comparing alternatives it is useful to control the conditions under which the experiments are performed so direct comparisons can be made. This is difficult when experimenting with the real system. For instance, it is not possible to control the arrival of patients at a hospital. It is also likely that experimentation with the real system will lead to the Hawthorne effect, where staff performance improves simply because some attention is being paid to them. In some cases the real system only occurs once, for example, a military campaign, and so there is no option to repeat an experiment. With a simulation model the conditions under which an experiment is performed can be repeated many times. The same pattern of patient arrivals can be generated time and time again, or the events that occur during a military campaign can be reproduced exactly as often as is required.
- *The real system does not exist.* A most obvious difficulty with real world experimentation is that the real system may not yet exist. Apart from building a series of alternative real world systems, which is unlikely to be practical in any but the most trivial of situations, direct experimentation is impossible in such circumstances. The only alternative is to develop a model.

Simulation versus other modelling approaches

Simulations are not the only models that can be used for understanding and improving the real world. Other modelling approaches range from simple paper calculations, through spreadsheet models, to more complex mathematical programming and heuristic methods (e.g. linear programming, dynamic programming, simulated annealing and genetic algorithms). Queuing theory provides a specific class of model that looks at similar situations to those often represented by simulations, arrivals, queues and service processes (Winston 1994). There are some reasons why simulation would be used in preference to these other methods.

- *Modelling variability.* It has already been stated that simulations are able to model variability and its effects. Meanwhile, many of the methods mentioned above are not able to do so. (It should be noted that some modelling approaches can be adapted to account for variability, but this often increases their complexity.) If the systems being modelled are subject to significant levels of variability, then simulation is often the only means for accurately predicting performance. Some systems cannot be modelled analytically. This is illustrated by Robinson and Higton (1995) who contrast the results from a “static” analysis of alternative factory designs with a simulation. In the static analysis the variability, largely resulting from equipment failures, was accounted for by averaging their effects into the process cycle times. In the simulation, the variability was modelled in detail. Whilst the static analysis predicted each design would reach the throughput required, the simulation showed that none of the designs were satisfactory. It is vital that variability is properly accounted for when attempting to predict performance.
- *Restrictive assumptions.* Simulation requires few, if any, assumptions, although the desire to simplify models and a shortage of data mean that some appropriate assumptions are normally made. Many other modelling approaches require certain assumptions. Queuing theory, for instance, often assumes particular distributions for arrival and service times. For many processes these distributions are not appropriate. In simulation, any distribution can be selected.
- *Transparency.* A manager faced with a set of mathematical equations or a large spreadsheet may struggle to understand, or believe, the results from the model. Simulation is appealing because it is more intuitive and an animated display of the system can be created, giving a non-expert greater understanding of, and confidence in, the model.

Of course, there are occasions when another modelling approach is appropriate and simulation is not required. Because simulation is a time consuming approach, it is recommended that it is used as a means of last resort, rather than the preferred option (Pidd 1998). That said, simulation is often the only resort. Indeed, surveys of modelling practice demonstrate that simulation is one of the most commonly used modelling techniques (Jeffrey and Seaton 1995; Fildes and Ranyard 1997; Clark 1999).

Simulation: the management perspective

Among the most compelling reasons for using simulation are the benefits that are gained by managers.

- *Fostering creativity.* “Ideas which can produce considerable improvements are often never tried because of an employee’s fear of failure” (Gogg and Mott 1992). With a simulation, however, ideas can be tried in an environment that is free of risk. This can only help to encourage creativity in tackling problem situations.
- *Creating knowledge and understanding.* At the end of many months of simulation modelling, the manager of the organization informed me that all of the benefits could have been obtained without the use of simulation by simply thinking about the problem in more detail. My defence lay in the fact that they would not have thought through the issues had the simulation not been there to act as a catalyst. The development and use of a simulation model forces people to think through issues that otherwise may not have been considered. The modeller seeks information, asks for data and questions assumptions, all of which lead to an improved knowledge and understanding of the system that is being simulated. Shannon (1975) recognizes that the development of the model alone, without the need for experimentation, may create sufficient understanding to bring about the necessary improvement to the real system. As the old adage states “a problem stated is a problem half solved”.
- *Visualization and communication.* Many good ideas have been trampled under foot because the benefits could not be demonstrated to a senior manager. Visual simulations prove a powerful tool for communication. It may be that an idea has already been proven but it is deemed necessary to build a simulation model in order to convince senior managers and colleagues of its validity.
- *Consensus building.* Many simulation studies are performed in the light of differing opinions as to the way forward. In the health sector, clinicians may be at odds with managers over the resources required. In a factory, managers and workers may not be in agreement over working hours and shifts. Sitting opposing parties around a simulation model of the problem situation can be a powerful means of sharing concerns and testing ideas with a view to obtaining a consensus of opinion.

1.3.3 The disadvantages of simulation

There are a number of problems with using simulation and these must not be ignored when deciding whether or not it is appropriate.

- *Expensive.* Simulation software is not necessarily cheap and the cost of model development and use may be considerable, particularly if consultants have to be employed.
- *Time consuming.* It has already been stated that simulation is a time consuming approach. This only adds to the cost of its use and means that the benefits are not immediate.
- *Data hungry.* Most simulation models require a significant amount of data. This is not always immediately available and, where it is, much analysis may be required to put it in a form suitable for the simulation.
- *Requires expertise.* Simulation modelling is more than the development of a computer program or the use of a software package. It requires skills in, among other things, conceptual modelling, validation and statistics, as well as skills in working with people and project management. These are the skills that are discussed in this book. This expertise is not always readily available.

- *Overconfidence*. There is a danger that anything produced on a computer is seen to be right. With simulation this is further exacerbated with the use of an animated display, giving an appearance of reality. When interpreting the results from a simulation, consideration must be given to the validity of the underlying model and the assumptions and simplifications that have been made.

1.4 When to Simulate

In general terms simulation, at least as it is described in this book, is used for modelling queuing systems. These consist of entities being processed through a series of stages, with queues forming between each stage if there is insufficient processing capacity. On the surface this may seem to be a limited set of circumstances, but the applications are many and various. Many systems can be conceived as queuing systems, whether it is people, physical items or information that are represented by the entities moving through the system.

It is impossible to give a full list of applications for which simulation might be used. It is, however, useful to give some indication of the range of systems that can be modelled. Banks *et al.* (1996) suggest the following list:

- Manufacturing systems
- Public systems: health care, military, natural resources
- Transportation systems
- Construction systems
- Restaurant and entertainment systems
- Business process reengineering/management
- Food processing
- Computer system performance

There are no doubt other applications that can be added to this list, for instance, service and retail systems.

1.5 Conclusion

This chapter discusses the nature of simulation that is described in this book. While a specific definition of simulation for modelling operations systems is provided, it is also shown that the term “simulation” has many meanings. The reasons for using simulation are discussed based on the nature of operations systems and the advantages of simulation. The latter describes why simulation is often preferable to other improvement approaches that could be adopted. The disadvantages of simulation are also identified. Finally, some common application areas for simulation modelling are listed. Having set the scene, the next chapter describes how a simulation model works by showing how the progression of time and variability are modelled.

Exercises

- E1.1 Think of situations where simulation could be used, for instance, from day-to-day life, a place of study or work. What aspects of each situation make simulation appropriate?
- E1.2 Take a typical operations system, preferably one that can be observed (e.g. a bank or supermarket), and identify the elements of variability, interconnectedness and complexity.
- E1.3 There are many case studies describing the application of simulation to real problems. Obtain and read some simulation case studies. Why was simulation used? What benefits were obtained? Some journals that often publish simulation case studies are: IIE Solutions, Interfaces, OR Insight and the Journal of the Operational Research Society. The Winter Simulation Conference proceedings (www.wintersim.org) include many case studies. Simulation software suppliers also publish case studies on their web sites (Section 3.3.3).

References

- Banks, J., Carson, J.S. and Nelson, B.L. (1996) *Discrete-Event System Simulation*, 2nd edn. Upper Saddle River, NJ: Prentice-Hall.
- Brooks, R.J. and Tobias, A.M. (1996) "Choosing the best model: level of detail, complexity and model performance". *Mathematical and Computer Modelling*, 24(4), 1–14.
- Checkland, P. (1981) *Systems Thinking, Systems Practice*. Chichester, UK: Wiley.
- Clark, D.N. (1999) "Strategic level MS/OR tool usage in the United Kingdom and New Zealand: a comparative survey". *Asia-Pacific Journal of Operational Research*, 16(1), 35–51.
- Coyle, R.G. (1996) *System Dynamics Modelling: A Practical Approach*. London: Chapman & Hall.
- Fildes, R. and Ranyard, J.C. (1997). "Success and survival of operational research groups – a review". *Journal of the Operational Research Society*, 48(4), 336–360.
- Gell-Mann, M. (1994) *The Quark and the Jaguar: Adventures in the Simple and the Complex*. London: Abacus.
- Gogg, T. and Mott, J. (1992) *Improve Quality and Productivity with Simulation*. Palos Verdes Pnsl., CA: JMI Consulting Group.
- Jeffrey, P. and Seaton, R. (1995) "The use of operational research tools: a survey of operational research practitioners in the UK". *Journal of the Operational Research Society*, 46(7), 797–808.
- Law, A.M. and Kelton, W.D. (2000) *Simulation Modeling and Analysis*, 3rd edn. New York: McGraw-Hill.
- Pidd, M. (1998) *Computer Simulation in Management Science*, 4th edn. Chichester, UK: Wiley.
- Pidd, M. (2003) *Tools for Thinking: Modelling in Management Science*, 2nd edn. Chichester, UK: Wiley.
- Robinson, S. and Higton, N. (1995) "Computer simulation for quality and reliability engineering". *Quality and Reliability Engineering International*, 11, 371–377.
- Senge, P.M. (1990) *The Fifth Discipline: The Art and Practice of the Learning Organization*. London: Random House.
- Shannon, R.E. (1975) *Systems Simulation: The Art and Science*. Englewood Cliffs, NJ: Prentice-Hall.
- Sterman, J.D. (2000) *Business Dynamics: Systems Thinking and Modeling for a Complex World*. New York: McGraw-Hill.
- Wild, R. (2002) *Operations Management*, 6th edn. London: Continuum.
- Winston, W.L. (1994) *Operations Research: Applications and Algorithms*, 3rd edn. Belmont, CA: Duxbury Press.