

## Multivariable Model-Building

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# Multivariable Model-Building

A pragmatic approach to regression analysis  
based on fractional polynomials for  
modelling continuous variables

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